

Metric Prefixes

10 ³	10 ²	10 ¹	1	10 ⁻¹	10 ⁻²	10 ⁻³	10 ⁻⁴	10 ⁻⁵	10 ⁻⁶	10 ⁻⁷	10 ⁻⁸	10 ⁻⁹	10 ⁻¹⁰	10 ⁻¹¹	10 ⁻¹²
k	-	-	none	d	c	m	-	-	μ	-	-	n	-	-	p

Motion

Speed:

$$\text{speed: } v = \frac{d}{t}$$

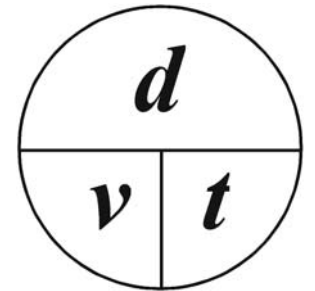
$$\text{distance: } d = vt$$

$$\text{time: } t = \frac{d}{v}$$

• v = speed

• d = distance

• t = time



Acceleration:

$$\text{acceleration: } a = \frac{\Delta v}{t} = \frac{v_f - v_i}{t}$$

$$\text{time: } t = \frac{v_f - v_i}{a}$$

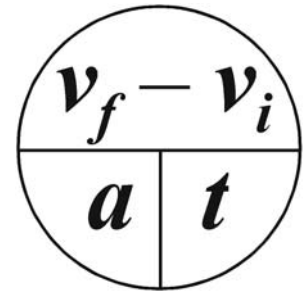
$$\text{final velocity: } v_f = v_i + at$$

• a = acceleration

• Δv = change in velocity

◦ v_f = final velocity

◦ v_i = initial velocity



Free Fall: (objects accelerating because of gravity)

$$\text{final speed: } v_f = gt + v_i$$

$$\text{distance: } d = \frac{1}{2}at^2 + v_i t$$

$$v_{avg} = \frac{v_f + v_i}{2}$$

• $g = a = 9.8 \text{ m/s}^2$ = acceleration of gravity

• d = distance

• t = time

• v_i = initial speed

• v_f = final speed

• v_{avg} = average speed

Units:

distance: m = meters; km = kilometers; cm = centimeters

time: h = hours; s = seconds

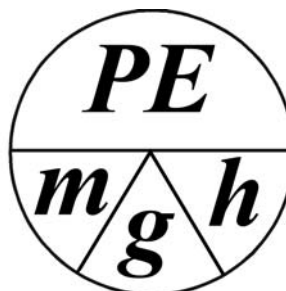
mass: g = grams; kg = kilograms

Energy

Gravitational Energy

$$PE = mgh$$

- The height from which the object falls (h)
- The mass of the object (m)
- The acceleration of gravity (g)



$$KE = \frac{1}{2}mv^2$$

- The mass of the object (m)
- The speed (v)

Force

Net Force:

Forces in the same direction

$$F_{net} = F_1 + F_2 + \dots + F_n$$

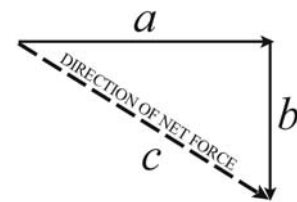
- $F_{net} = \text{net force}$
- $F_1 + F_2 + \dots + F_n = \text{add all the forces}$

Forces in opposite directions

$$F_{net} = F_L - F_S$$

- $F_L = \text{larger force}$
- $F_S = \text{smaller force}$
- $F_L - F_S = \text{subtract the forces}$

THE NET FORCE IS IN THE DIRECTION OF THE LARGER FORCE



Forces at right angles

Pythagorean theorem

$$a^2 + b^2 = c^2$$

$$c = \sqrt{c^2}$$

- $a = \text{one of the forces at right angles}$
- $b = \text{one of the forces at right angles}$
- $c = \text{the net force}$

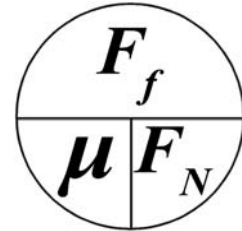
Multiple forces

Always add all the forces acting in the same direction before subtracting or applying the Pythagorean theorem

Coefficient of Friction

$$F_f = F_N \times \mu$$

- $F_f = \text{force of friction}$
- $F_N = \text{normal force}$
- $\mu = \text{coefficient of friction}$



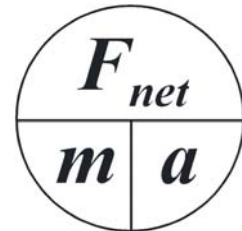
Newton's Second Law of Motion:

acceleration: $a = \frac{F}{m}$

force: $F = ma$ ($F = m \times a$)

mass: $m = \frac{F}{a}$

- $a = \text{acceleration}$
- $F = \text{force}$
- $m = \text{mass}$



Air Resistance:

$$F_{net} = F_{weight} - F_{air\ resistance}$$

$$F_{weight} = mg$$

- $F_{net} = \text{net force}$
- $F_{weight} = \text{weight}$
- $F_{air\ resistance} = \text{air resistance}$
- $m = \text{mass}$
- $g = \text{acceleration of gravity } (9.8\text{m/s}^2)$

Units:

distance: $m = \text{meters}; km = \text{kilometers}; cm = \text{centimeters}$

time: $h = \text{hours}; s = \text{seconds}$

mass: $g = \text{grams}; kg = \text{kilograms}$

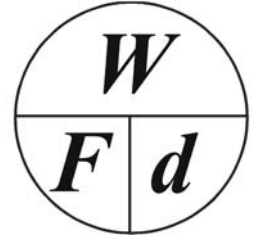
force: $N = \text{newtons}; 1N = 1 \frac{kg \cdot m}{s^2}$

Machines

Work:

$$W = F \times d$$

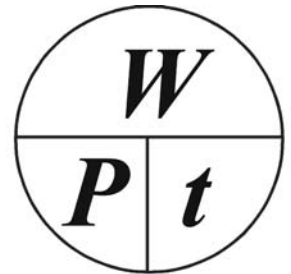
- W = work (J)
- F = force (N)
- d = distance (m)



Power:

$$Power = \frac{Work}{time}$$

$$P = \frac{W}{t}$$



Mechanical Advantage:

$$mechanical\ advantage = \frac{output\ force}{input\ force}$$

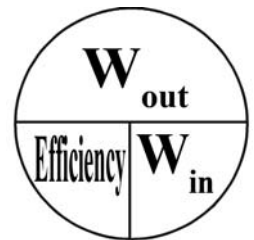
$$MA = \frac{F_{out}}{F_{in}}$$



Efficiency:

$$efficiency = \frac{work\ output}{work\ input} \times 100\%$$

$$eff = \frac{W_{out}}{W_{in}} \times 100\%$$



(NOTE: Express efficiency as a decimal to calculate W_{out} or W_{in} .)

Inclined Plane:

$$W_{out} = F_{out} \times D_{out}$$

$$W_{in} = F_{in} \times D_{in}$$

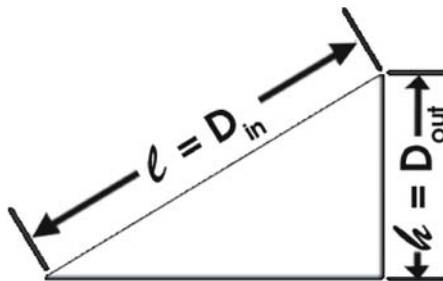
$$W_f = W_{in} - W_{out}$$

$$AMA = F_{out}/F_{in}$$

$$IMA = D_{in}/D_{out}$$

$$Eff = (W_{out}/W_{in}) \times 100$$

$$Eff = (AMA/IMA) \times 100$$



Machines (Continued)

Levers:

$$IMA = \frac{A_E}{A_R}$$

$$M = F \times A$$

$$M = M_1 + M_2 + \dots$$

Balanced levers

$$M_E = M_R$$

- IMA = ideal mechanical advantage
- A_E = effort arm
- A_R = resistance arm
- M_E = effort moment
- M_R = resistance moment



Wheel and Axle:

$$IMA = \frac{\text{input radius}}{\text{output radius}}$$

$$IMA = \frac{R_{in}}{R_{out}}$$



Pulleys:

$$IMA = \# \text{ of supporting strands}$$

$$IMA \text{ (fixed pulley)} = 1$$

$$IMA \text{ (movable pulley)} = 2$$



Units:

work: J = joules (also units for energy)

power: W = watts $1 W = 1 J/s$

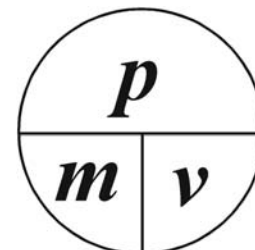
MA : no units

Momentum

Momentum:

$$p = mv$$

- p = momentum ($kg \cdot m/s$)
- m = mass (kg)
- v = velocity (m/s)
- p_{TOTAL} = total momentum
- p_1, p_2, p_n = momentums of the objects in a system



$$p_{TOTAL} = p_1 + p_2 + \dots + p_n$$

Change of Momentum and Force:

Definitions

$$\bullet F = ma$$

$$\bullet a = \frac{\Delta v}{t}$$

$$\bullet \Delta p = m\Delta v$$

Substitutions

$$F = \frac{m\Delta v}{t}$$

$$F = \frac{\Delta p}{t}$$

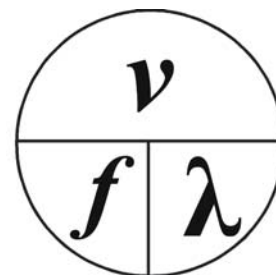


Waves

Speed:

$$v = f\lambda$$

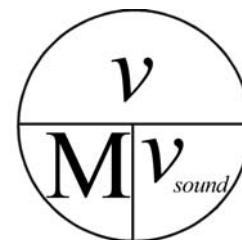
- v = speed (m/s)
- f = frequency ($1/s$ or Hz)
- λ = wavelength (m)



Sound

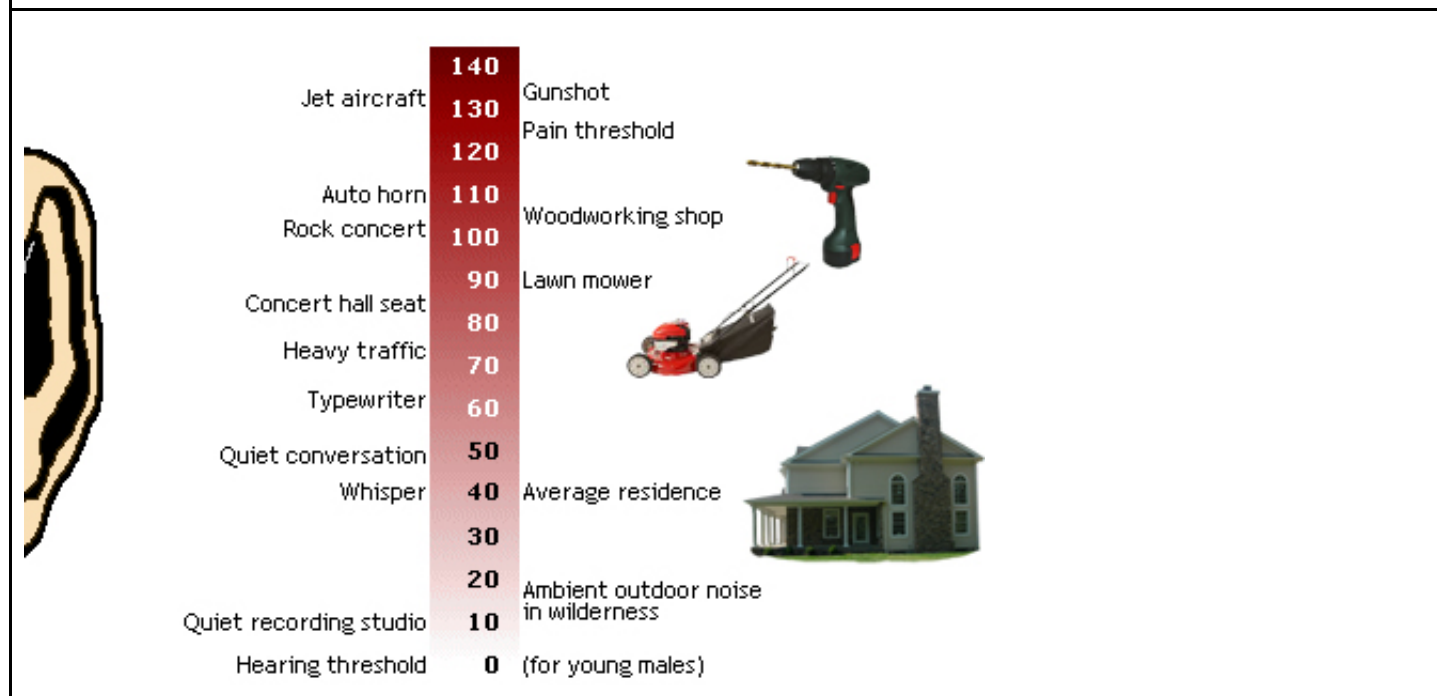
$$M = \frac{v}{v_{sound}}$$

- M = mach number
- v = speed relative to the medium
- v_{sound} = speed of sound in the medium



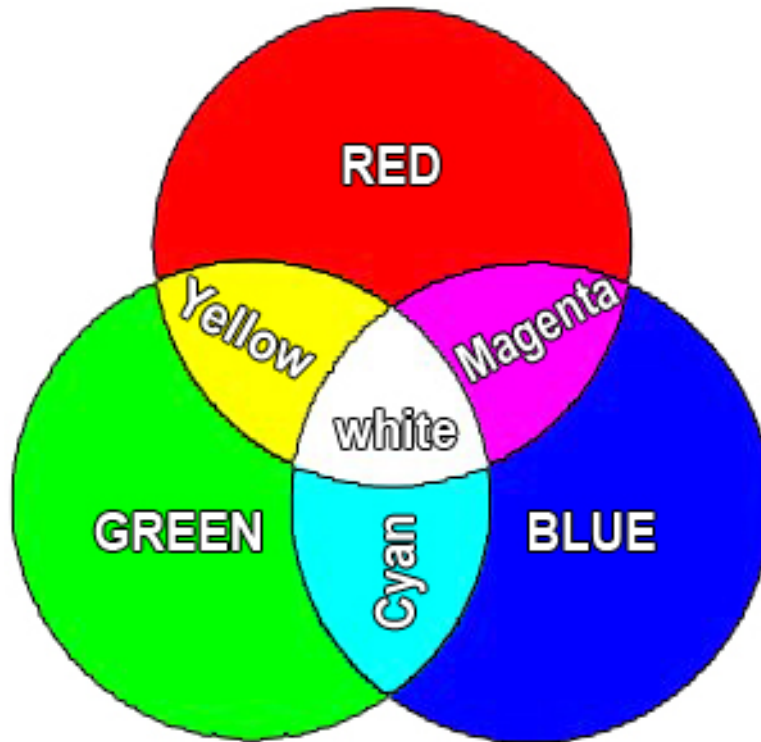
Speed of Sound Through Different Materials

Material	Speed (m/s)
Air	343
Water	1,483
Steel	5,940
Glass	5,640



Light

Primary Colors



Speed in a vacuum

Speed in a vacuum = $3.0 \times 10^8 \text{ m/s}$

Heat

Temperature:

$$K = C + 273$$

• $K = \text{Kelvins}$

$$C = K - 273$$

• $C = \text{Celsius } (^{\circ}\text{C})$

Heat:

$$q = mC\Delta T$$

• $q = \text{heat (joules)}$

• $T_f = \text{final temperature}$

• $C = \text{specific heat } \left(\frac{J}{g^{\circ}C} \text{ or } \frac{J}{gK} \right)$

• $T_i = \text{initial temperature}$

$$\Delta T = T_f - T_i$$

• $\Delta T = \text{temperature change}$



Specific Heats of Common Substances:

Material	Specific Heat (J/g°C)
water	4.18
aluminum	0.897
copper	0.385
lead	0.129
nickel	0.444
zinc	0.388

Units:

heat

$J = \text{joules}$

temperature

$^{\circ}C = \text{degrees Celsius; } K = \text{Kelvins}$

specific heat

$\frac{J}{g^{\circ}C} \text{ or } \frac{J}{gK} = \text{joules per gram degree Celsius or joules per gram Kelvin}$

Pressure and Fluids

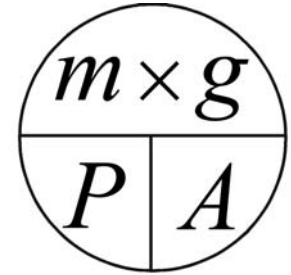
Pressure:

pressure: $P = \frac{F}{A}$

force: $F = PA$ ($F = P \times A$)

area: $A = \frac{F}{P}$

- $P =$ pressure
- $F =$ force
- $A =$ area



Archimedes' Principle:

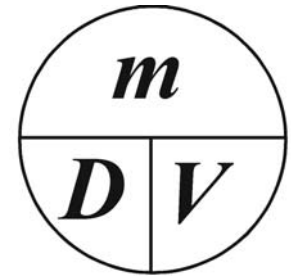
density: $D = \frac{m}{V}$

mass: $m = D \times V$

volume: $V = \frac{m}{D}$

$V = L \times W \times H$

- $D =$ density
- $m =$ mass
- $V =$ volume
- $L =$ length
- $W =$ width
- $H =$ height

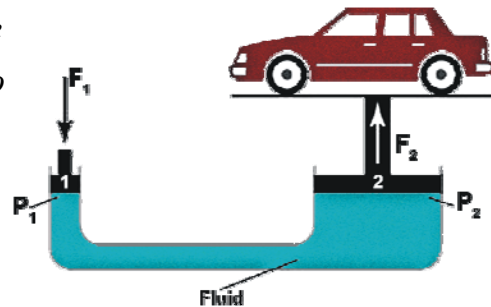


(NOTE: Density of water – 1 g/mL or 1 kg/L)

Pascal's Principle:

$$\frac{F_1}{A_1} = \frac{F_2}{A_2}$$

- $F_1 =$ force applied on surface one
- $F_2 =$ force applied on surface two
- $A_1 =$ area of surface one
- $A_2 =$ area of surface two



Units:

force: $N =$ newtons; $1N = 1 \frac{kg \cdot m}{s^2}$

pressure: $Pa =$ pascals

area: $m^2 =$ meters squared

volume: $m^3 =$ meters cubed; $cm^3 =$ centimeters cubed (note: 1 mL = 1 cm³); L = liters

Physical Constants

Name	Symbol	Value
Universal gravitational constant	G	$6.67 \times 10^{-11} \text{ N} \cdot \text{m}^2/\text{kg}^2$
Acceleration due to gravity	g	9.81 m/s^2
Speed of light in a vacuum	c	$3.00 \times 10^8 \text{ m/s}$
Speed of sound in air at STP		$3.31 \times 10^2 \text{ m/s}$
Mass of Earth		$5.98 \times 10^{24} \text{ kg}$
Mass of the Moon		$7.35 \times 10^{22} \text{ kg}$
Mean radius of Earth		$6.37 \times 10^6 \text{ m}$
Mean radius of the Moon		$1.74 \times 10^6 \text{ m}$
Mean distance—Earth to the Moon		$3.84 \times 10^8 \text{ m}$
Mean distance—Earth to the Sun		$1.50 \times 10^{11} \text{ m}$
Electrostatic constant	k	$8.99 \times 10^9 \text{ N} \cdot \text{m}^2/\text{C}^2$
1 elementary charge	e	$1.60 \times 10^{-19} \text{ C}$
1 coulomb (C)		6.25×10^{18} elementary charges
1 electronvolt (eV)		$1.60 \times 10^{-19} \text{ J}$
Planck's constant	h	$6.63 \times 10^{-34} \text{ J} \cdot \text{s}$
1 universal mass unit (u)		$9.31 \times 10^2 \text{ MeV}$
Rest mass of the electron	m_e	$9.11 \times 10^{-31} \text{ kg}$
Rest mass of the proton	m_p	$1.67 \times 10^{-27} \text{ kg}$
Rest mass of the neutron	m_n	$1.67 \times 10^{-27} \text{ kg}$

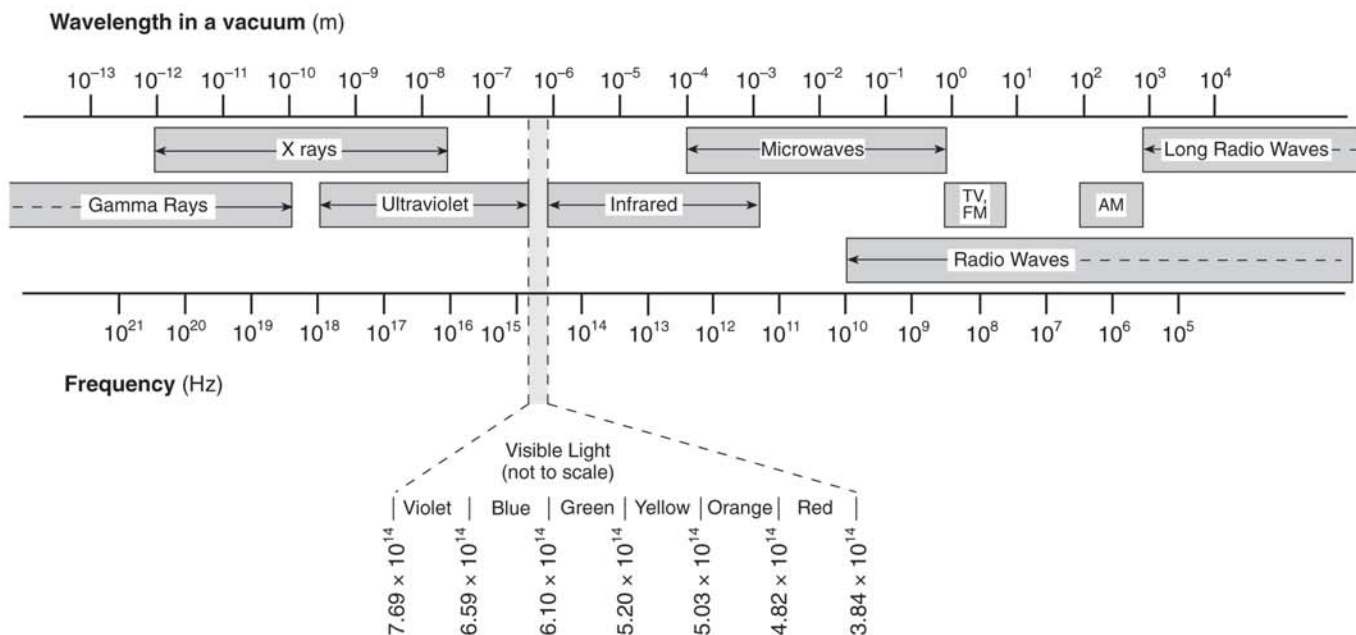
Prefixes for Powers of 10

Prefix	Symbol	Notation
tera	T	10^{12}
giga	G	10^9
mega	M	10^6
kilo	k	10^3
deci	d	10^{-1}
centi	c	10^{-2}
milli	m	10^{-3}
micro	μ	10^{-6}
nano	n	10^{-9}
pico	p	10^{-12}

Approximate Coefficients of Friction

	Kinetic	Static
Rubber on concrete (dry)	0.68	0.90
Rubber on concrete (wet)	0.58	
Rubber on asphalt (dry)	0.67	0.85
Rubber on asphalt (wet)	0.53	
Rubber on ice	0.15	
Waxed ski on snow	0.05	0.14
Wood on wood	0.30	0.42
Steel on steel	0.57	0.74
Copper on steel	0.36	0.53
Teflon on Teflon	0.04	

The Electromagnetic Spectrum



Absolute Indices of Refraction	
$(f = 5.09 \times 10^{14} \text{ Hz})$	
Air	1.00
Corn oil	1.47
Diamond	2.42
Ethyl alcohol	1.36
Glass, crown	1.52
Glass, flint	1.66
Glycerol	1.47
Lucite	1.50
Quartz, fused	1.46
Sodium chloride	1.54
Water	1.33
Zircon	1.92

Waves

$$v = f\lambda$$

$$T = \frac{1}{f}$$

$$\theta_i = \theta_r$$

$$n = \frac{c}{v}$$

$$n_1 \sin \theta_1 = n_2 \sin \theta_2$$

$$\frac{n_2}{n_1} = \frac{v_1}{v_2} = \frac{\lambda_1}{\lambda_2}$$

c = speed of light in a vacuum

f = frequency

n = absolute index of refraction

T = period

v = velocity or speed

λ = wavelength

θ = angle

θ_i = angle of incidence

θ_r = angle of reflection

Modern Physics

$$E_{\text{photon}} = hf = \frac{hc}{\lambda}$$

$$E_{\text{photon}} = E_i - E_f$$

$$E = mc^2$$

c = speed of light in a vacuum

E = energy

f = frequency

h = Planck's constant

m = mass

λ = wavelength

Geometry and Trigonometry

Rectangle

$$A = bh$$

A = area

b = base

Triangle

$$A = \frac{1}{2}bh$$

C = circumference

h = height

r = radius

Circle

$$A = \pi r^2$$

$$C = 2\pi r$$

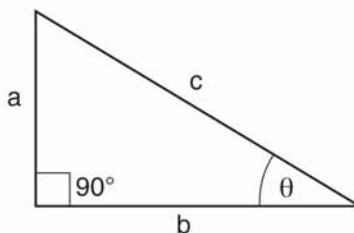
Right Triangle

$$c^2 = a^2 + b^2$$

$$\sin \theta = \frac{a}{c}$$

$$\cos \theta = \frac{b}{c}$$

$$\tan \theta = \frac{a}{b}$$



Mechanics

$$\bar{v} = \frac{d}{t}$$

$$a = \frac{\Delta v}{t}$$

$$v_f = v_i + at$$

$$d = v_i t + \frac{1}{2} at^2$$

$$v_f^2 = v_i^2 + 2ad$$

$$A_y = A \sin \theta$$

$$A_x = A \cos \theta$$

$$a = \frac{F_{net}}{m}$$

$$F_f = \mu F_N$$

$$F_g = \frac{Gm_1m_2}{r^2}$$

$$g = \frac{F_g}{m}$$

$$p = mv$$

$$p_{before} = p_{after}$$

$$J = F_{net} t = \Delta p$$

$$F_s = kx$$

$$PE_s = \frac{1}{2} kx^2$$

$$F_c = ma_c$$

$$a_c = \frac{v^2}{r}$$

$$\Delta PE = mg\Delta h$$

$$KE = \frac{1}{2} mv^2$$

$$W = Fd = \Delta E_T$$

$$E_T = PE + KE + Q$$

$$P = \frac{W}{t} = \frac{Fd}{t} = F\bar{v}$$

a = acceleration

a_c = centripetal acceleration

A = any vector quantity

d = displacement or distance

E_T = total energy

F = force

F_c = centripetal force

F_f = force of friction

F_g = weight or force due to gravity

F_N = normal force

F_{net} = net force

F_s = force on a spring

g = acceleration due to gravity or
gravitational field strength

G = universal gravitational constant

h = height

J = impulse

k = spring constant

KE = kinetic energy

m = mass

p = momentum

P = power

PE = potential energy

PE_s = potential energy stored in a spring

Q = internal energy

r = radius or distance between centers

t = time interval

v = velocity or speed

\bar{v} = average velocity or average speed

W = work

x = change in spring length from the
equilibrium position

Δ = change

θ = angle

μ = coefficient of friction

Standard Temperature and Pressure

Name	Value	Unit
Standard Pressure	101.3 kPa 1 atm	kilopascal atmosphere
Standard Temperature	273 K 0°C	kelvin degree Celsius

Physical Constants for Water

Heat of Fusion	334 J/g
Heat of Vaporization	2260 J/g
Specific Heat Capacity of H ₂ O(ℓ)	4.18 J/g•K

Selected Units

Symbol	Name	Quantity
m	meter	length
g	gram	mass
Pa	pascal	pressure
K	kelvin	temperature
mol	mole	amount of substance
J	joule	energy, work, quantity of heat
s	second	time
min	minute	time
h	hour	time
d	day	time
y	year	time
L	liter	volume
ppm	parts per million	concentration
M	molarity	solution concentration
u	atomic mass unit	atomic mass