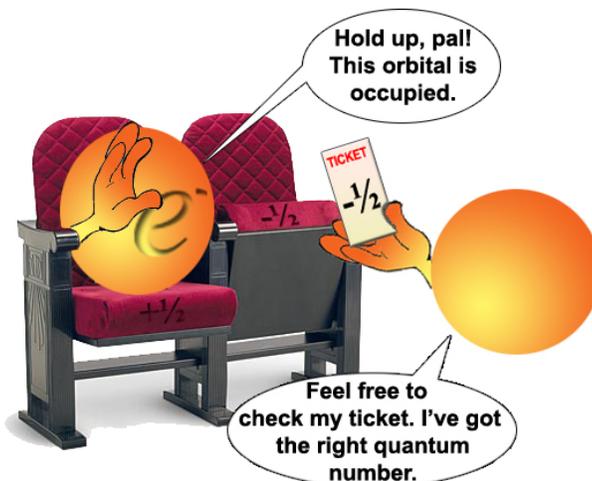


## Quantum Numbers

Orbitals are characterized by a series of quantum numbers that describe them. The **principal** quantum number,  $n$ , or energy level is similar to the shells of the Bohr model. The principal quantum number has integral values from 1 through 7. These correspond to the period numbers in periodic table, and are related to the size and energy of the orbital. As  $n$  increases, the orbital becomes larger, and the electron spends more time further away from the nucleus. As a result, the electron is less tightly bound to the nucleus and has higher energy. The **angular momentum** quantum number ( $\ell$ ) corresponds to the subshells, divisions of principal energy levels. Angular momentum relates to the shape of the orbitals. For example, an orbital with an angular momentum of  $\ell = 0$  has no nodes (areas of zero probability of finding an electron within an orbital) and looks spherical, while an orbital with an angular momentum of  $\ell = 1$  has one node and looks like a figure eight. Angular momentum has integral values from 0 to  $n-1$ . As a result the maximum number of subshells in a principal energy level is  $n$ . None of the existing elements uses more than 4 subshells even in principal energy levels 4 through 7. Subshells are designated by letters:  $\ell = 0$  is called  $s$ ,  $\ell = 1$  is called  $p$ ,  $\ell = 2$  is called  $d$ , and  $\ell = 3$  is called  $f$ . The subshells in increasing order of energy are  $s$ ,  $p$ ,  $d$ , and  $f$ . The energy of an electron can be described by its principal energy level and its subshell. The first principal energy level has one subshell,  $1s$ . The second principal energy level has two subshells,  $2s$  and  $2p$ . The third principal energy level has three subshells,  $3s$ ,  $3p$ , and  $3d$ . The fourth principal energy level has four subshells,  $4s$ ,  $4p$ ,  $4d$ , and  $4f$ . The **magnetic** quantum number ( $m_\ell$ ) has integral values between  $\ell$  and  $-\ell$  including 0. The value of  $m_\ell$  is related to the orientation of the orbital in space relative to the other orbitals of the atom. Spectral data indicate that electrons have a magnetic moment or *spin* with two possible orientations when placed in an external magnetic field. The **electron spin** quantum number ( $m_s$ ) can have only one of two values,  $+\frac{1}{2}$ , or  $-\frac{1}{2}$ . Wolfgang Pauli concluded, in a given atom, no two electrons can have the same four quantum numbers (**the Pauli Exclusion Principle**). Any electrons in the same orbital will have the same principal quantum number ( $n$ ), the same angular momentum ( $\ell$ ), and the same magnetic quantum number ( $m_\ell$ ). By the Pauli exclusion principle, they must have different spins to occupy the same orbital. Since there are only two spins, the maximum number of electrons in an orbital is 2.



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Answer the questions below based on your knowledge of the reading above, and on your knowledge of chemistry.

1. What are the quantum numbers for the valence electrons of calcium? \_\_\_\_\_
2. For a  $d$  sublevel:
  - a. What is the angular momentum quantum number? \_\_\_\_\_
  - b. How many nodes do the orbitals have? \_\_\_\_\_
  - c. What are the possible magnetic quantum numbers? \_\_\_\_\_
  - d. How many  $d$  orbitals are there? \_\_\_\_\_
  - e. What are the possible electron spin quantum numbers for  $d$  electrons? \_\_\_\_\_
  - f. What is the maximum number of  $d$  electrons? \_\_\_\_\_